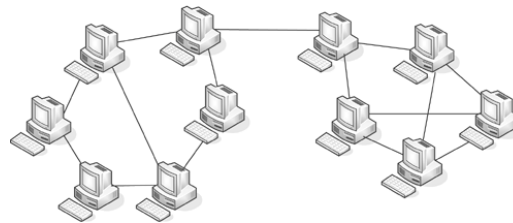


Decentralized query reformulation in DL-Lite (IJCAI 2009)



Marie-Christine Rousset

Université Grenoble & CNRS(LIG)

Joint work with Nada Abdallah and François Goasdoué

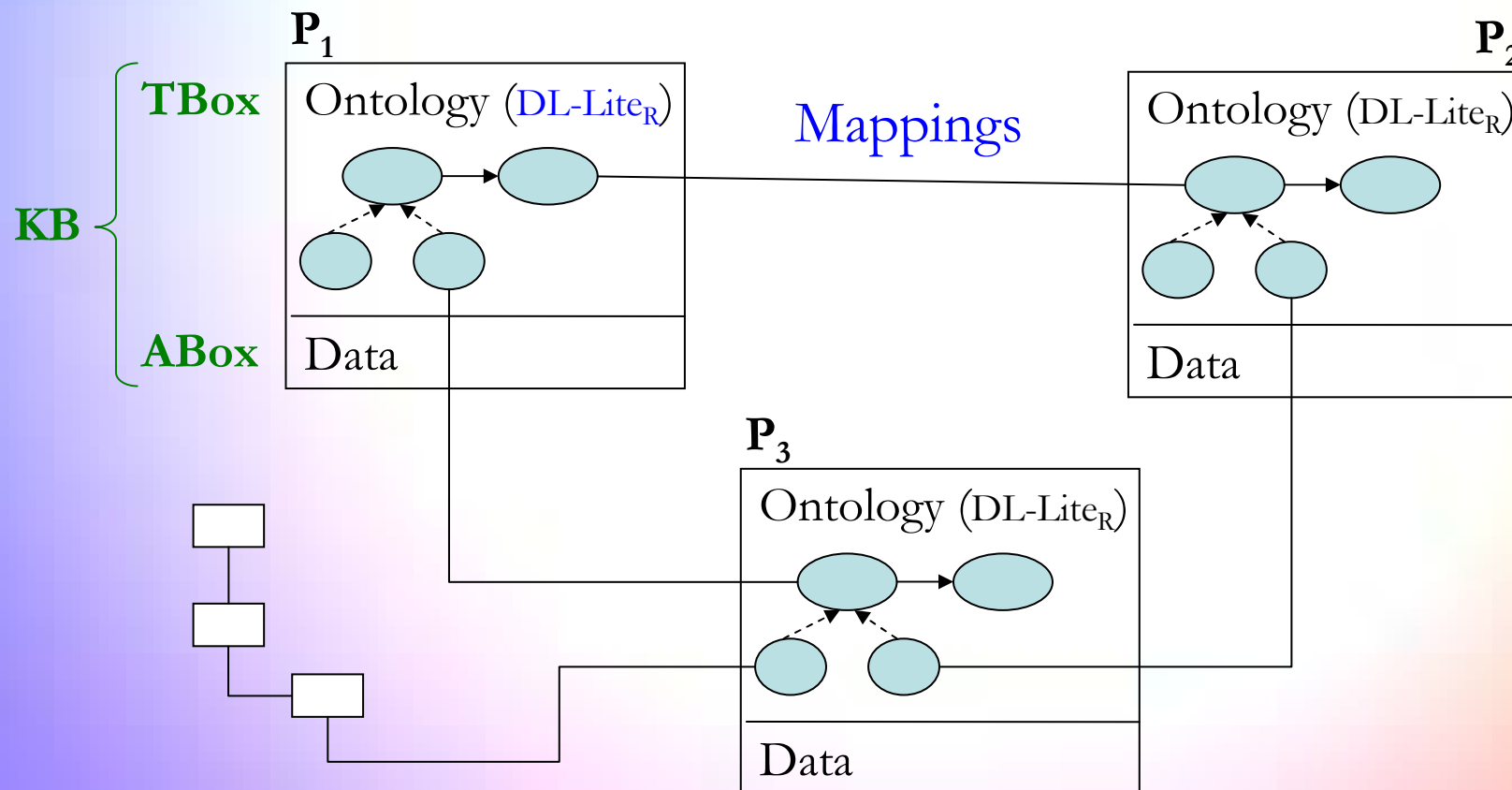
Université Paris-Sud & CNRS(LRI/IASI) – INRIA (Saclay/LEO)

Setting

Decentralized data management for the Semantic Web

Decentralized: Dynamic network of collaborative peers

Semantic Web: Data are described with ontologies (OWL2)

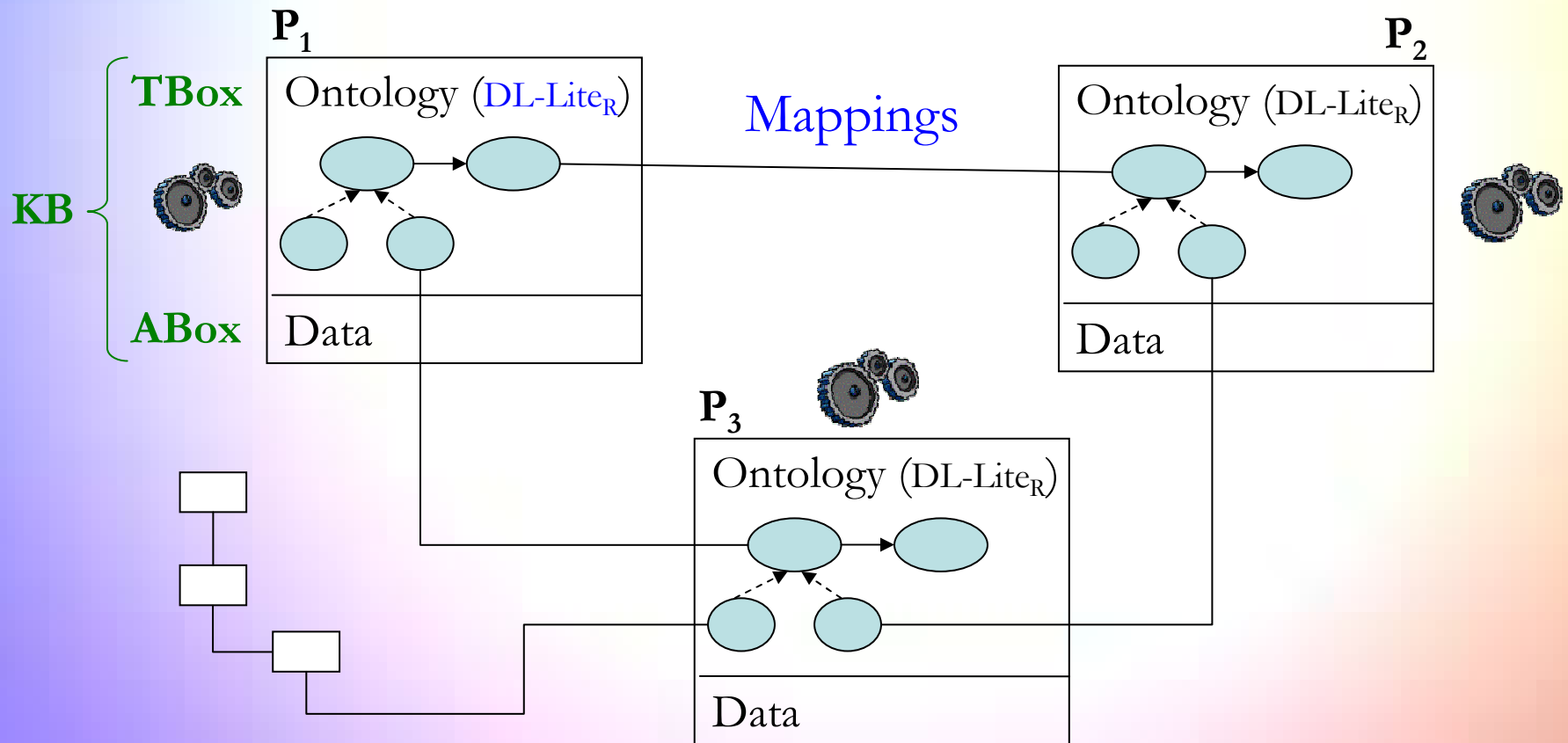


Context Decentralized Data management system for the Semantic Web

Decentralized: Dynamic Network of collaborative peers

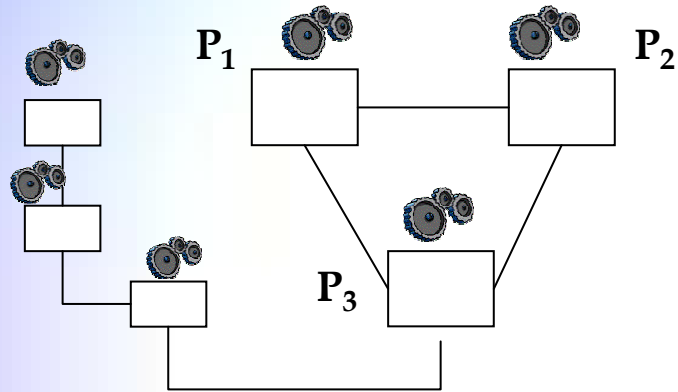
Semantic Web: Data are described with ontologies (OWL2)

Global knowledge unknown



Contributions

1. DL-Lite_R decentralized data model

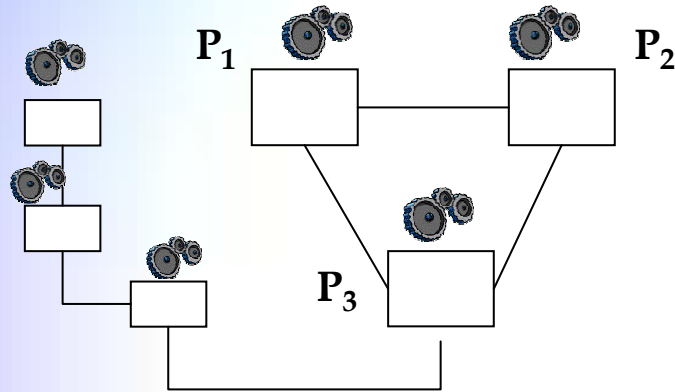


2. Decentralized Algorithms for:

- ✓ Data consistency checking
- ✓ Query Answering

Contributions

1. DL-Lite_R decentralized data model



2. Decentralized Algorithms for:

- ✓ Data consistency checking
- ✓ Query Answering

State of the art

- D. Calvese and al. (JAR 07)
“Tractable reasoning and efficient query answering in description logics”

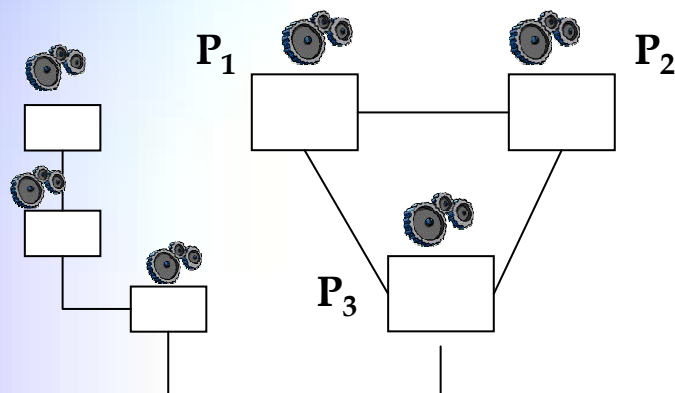
Centralized
DL-Lite_R KB

Centralized Algorithms for:

- ✓ Data consistency checking
- ✓ Query Answering

Contributions

1. DL-Lite_R decentralized data model



2. Decentralized Algorithms for:

- ✓ Data consistency checking
- ✓ Query Answering by reformulation

3. Decentralized & Centralized Algorithms for:

- ✓ View consistency checking
- ✓ Query Answering using views

State of the art

- D.Calvenese and al. (JAR 07)
“Tractable reasoning and efficient query answering in description logics”

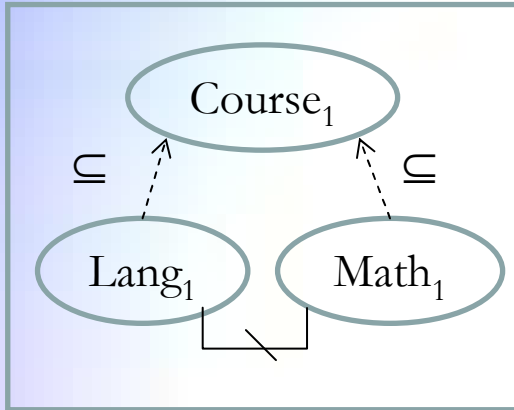
Centralized
DL-Lite_R KB

Centralized Algorithms for:

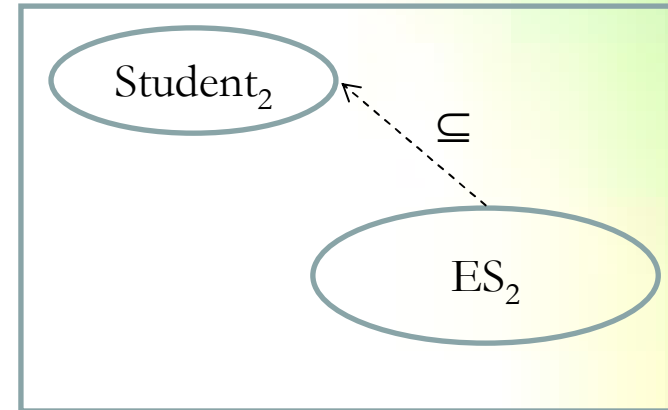
- ✓ Data consistency checking
- ✓ Query Answering by reformulation

DL-Lite_R decentralized data management: illustration

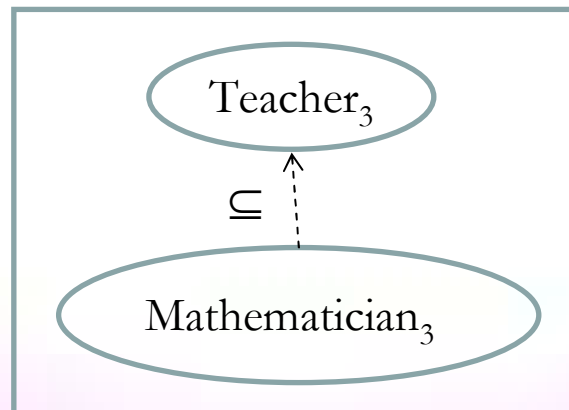
P₁



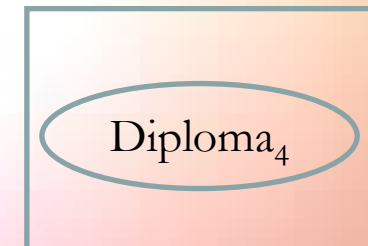
P₂



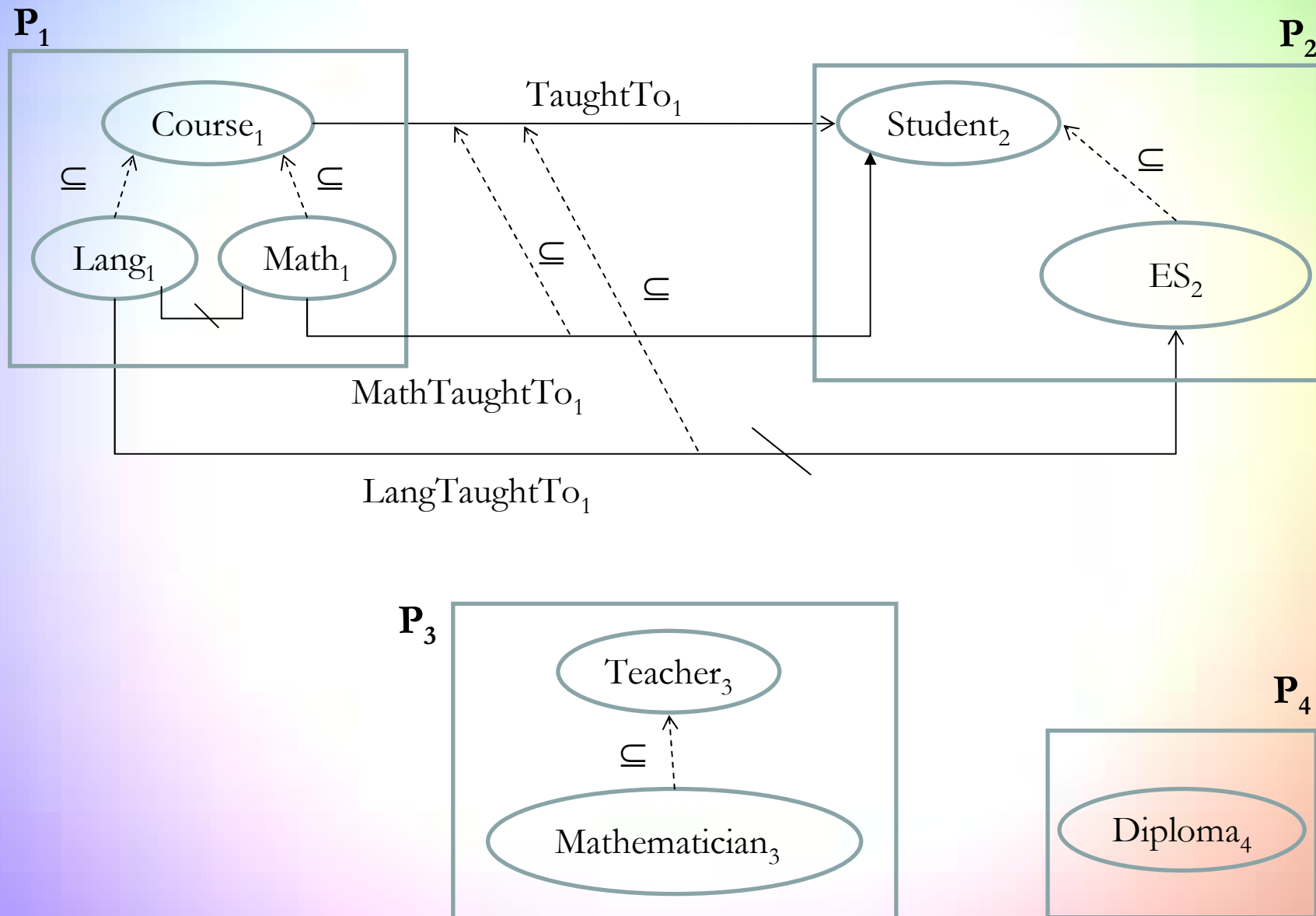
P₃



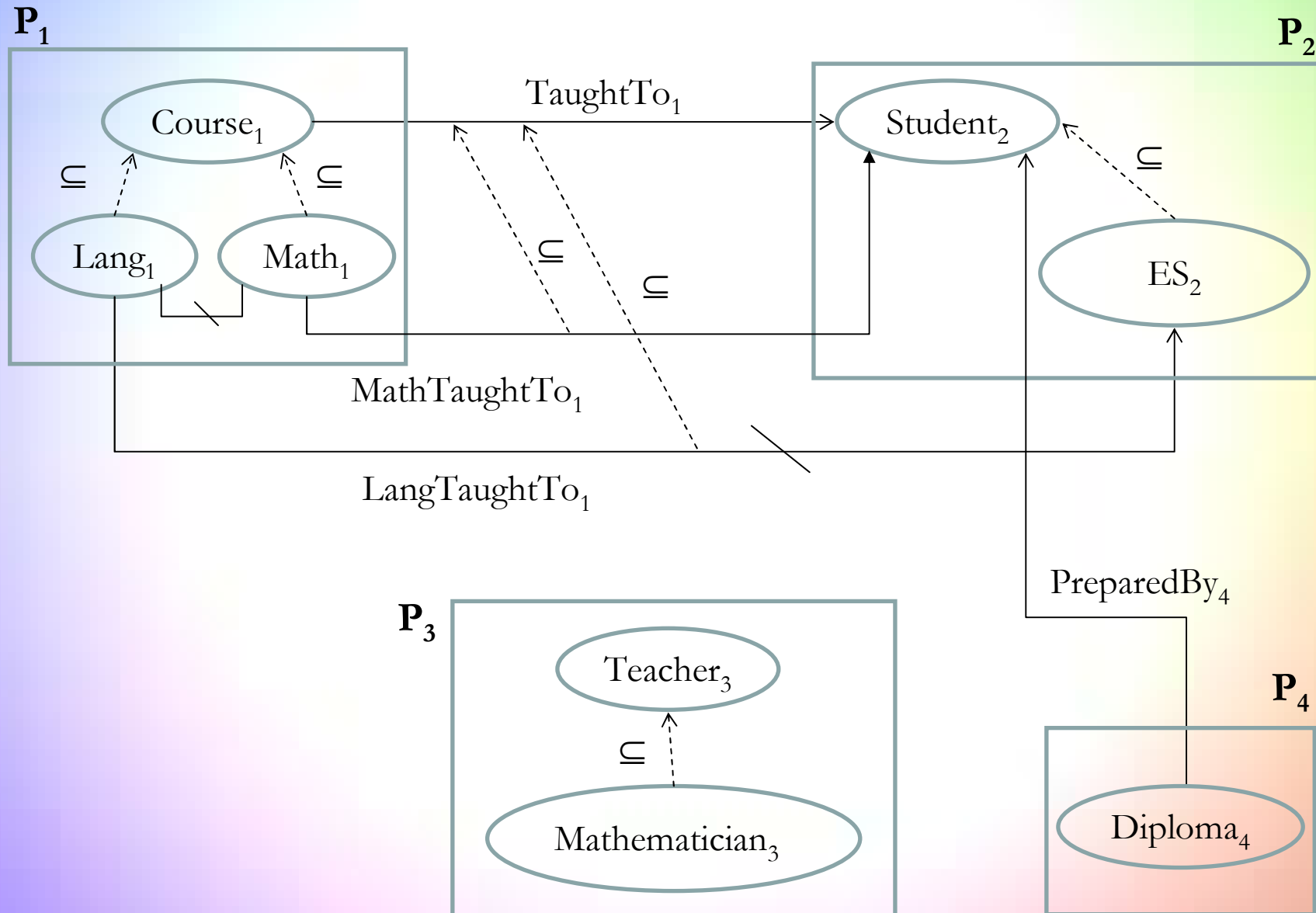
P₄



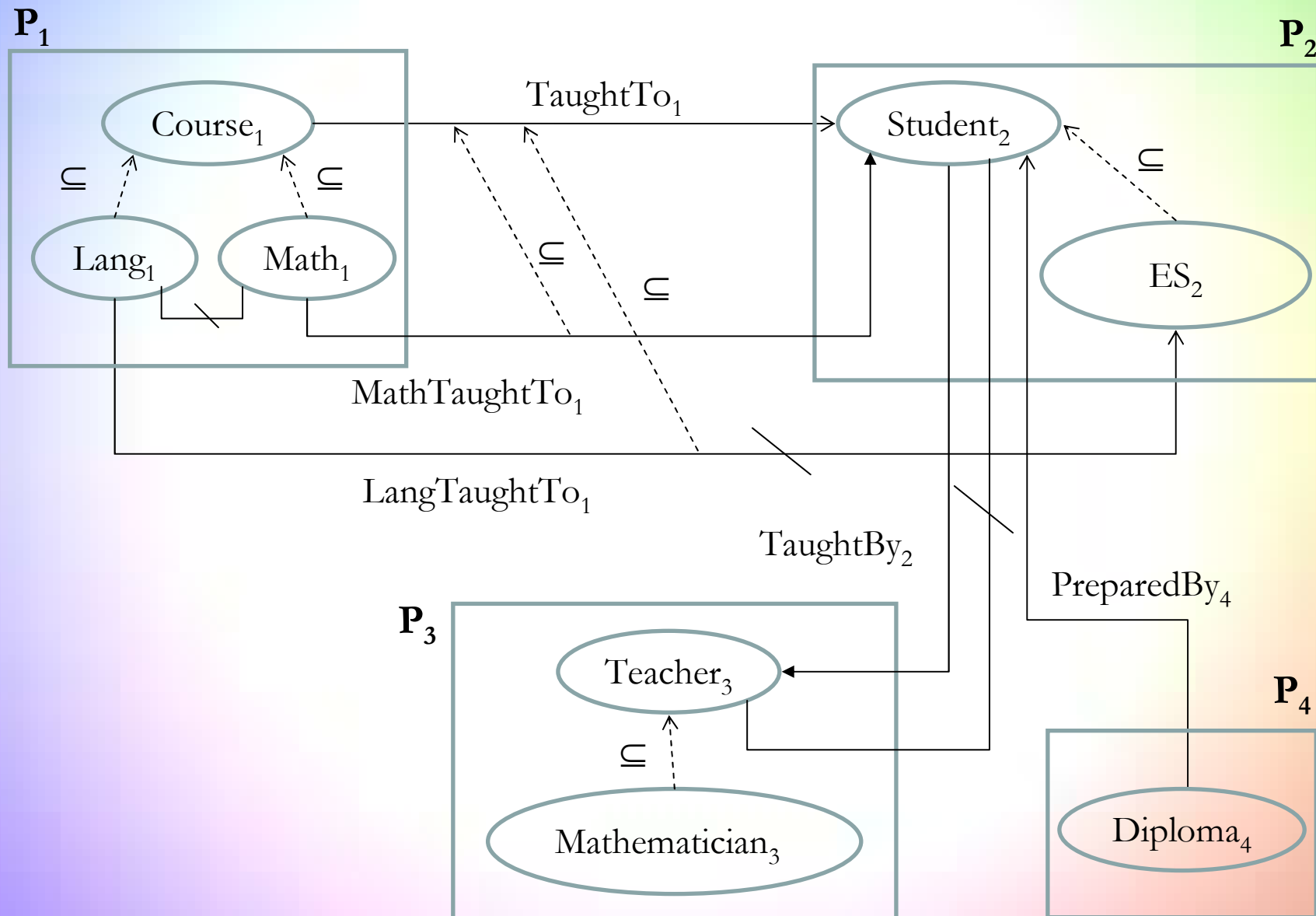
DL-Lite_R decentralized data management system



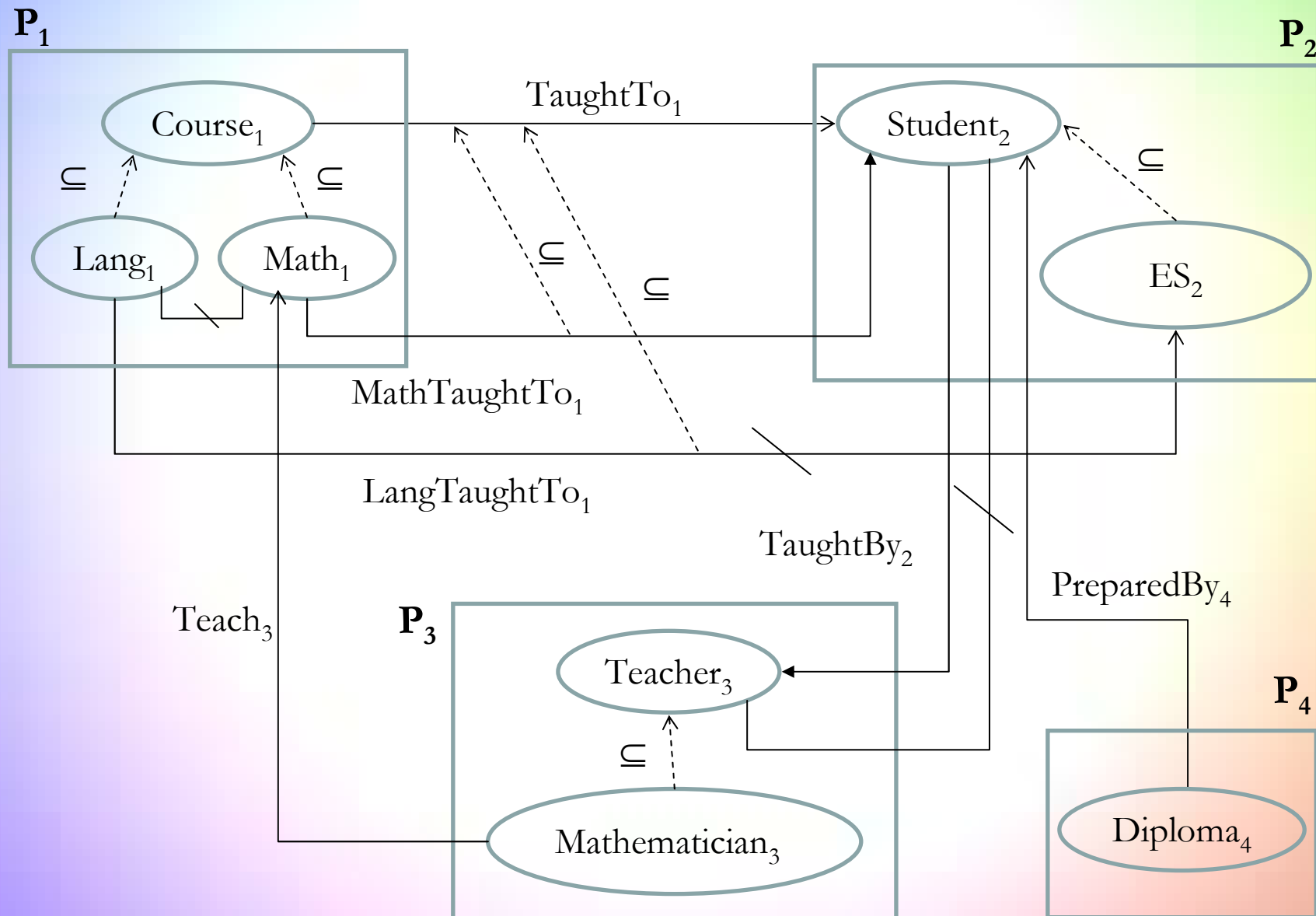
DL-Lite_R decentralized data management system



DL-Lite_R decentralized data management system

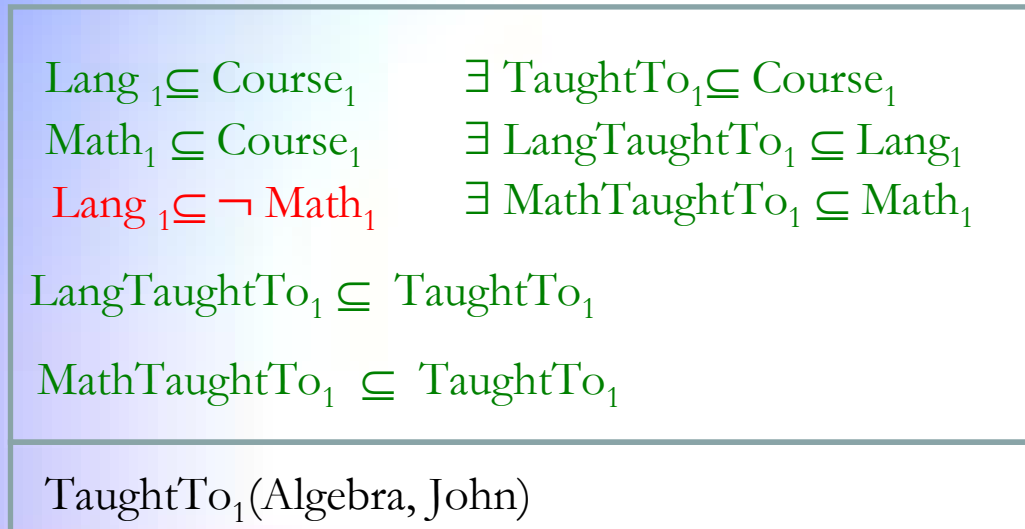


DL-Lite_R decentralized data management system



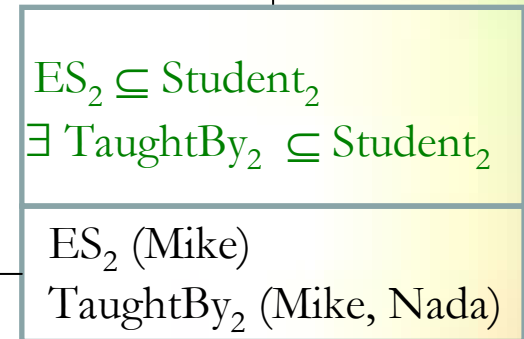
DL-Lite_R decentralized data management system

P₁



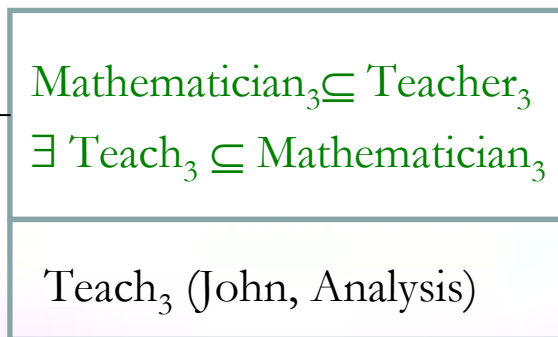
∃ TaughtTo₁ ⊆ Student₂
 ∃ LangTaughtTo₁ ⊆ ¬ ES₂
 ∃ MathTaughtTo₁ ⊆ Student₂

P₂



∃ TaughtBy₂ ⊆ Teacher₃
 Student₂ ⊆ ¬ Teacher₃

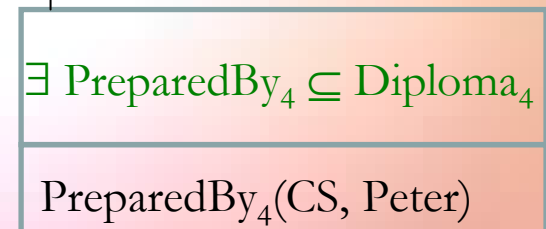
P₃



∃ Teach₃ ⊆ Course₁

∃ PreparedBy₄ ⊆ Student₂

P₄



Data consistency Checking

- Consistency problem:

A data management system is consistent iff its KB (Tbox + Abox) is satisfiable.

- In DL-Lite_R :

- ✓ Tbox is always satisfiable
- ✓ Tbox + Abox may be insatisfiable

- Example :

TBox	$\exists \text{TaughtTo}_1 \subseteq \text{Student}_2$ $\text{Student}_2 \subseteq \neg \text{Teacher}_3$ $\text{Mathematician}_3 \subseteq \text{Teacher}_3$ $\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$	<p>Implicit Negative Inclusion</p> <p>↑</p> $\text{TBox} \not\models \exists \text{TaughtTo}_1 \subseteq \neg \exists \text{Teach}_3$	$\left. \vphantom{\begin{matrix} \text{TBox} \\ \text{KB} \end{matrix}} \right\} \perp$
ABox	$\text{TaughtTo}_1 (\text{Algebra}, \text{John})$ $\text{Teach}_3 (\text{John}, \text{Analysis})$	$\text{KB} \models \exists y \text{TaughtTo}_1 (y, \text{John})$ $\text{KB} \models \exists y \text{Teach}_3 (\text{John}, y)$	

Data consistency Checking

- Centralized case

Existing Algorithm Consistent :

D.Calvenese and al. (JAR 07) :“Tractable reasoning and efficient query answering in description logics”

- Computes all the Negative Inclusions entailed by the Tbox.
- Checks if the computed negative inclusions are violated by the Abox.

Checking if the DL-Lite_R formulae that must be disjoint according to the TBox, indeed have disjoint instances in the Abox

Data consistency Checking

- Decentralized case

- Decentralized Data consistency Checking w.r.t a peer

- ✓ Each peer propagates over the network each of its positive or negative inclusions and collects in return all the negative inclusions of the network **the entailment of which uses the Tbox of the peer.**
 - All Negative Inclusions entailed by the network are not necessarily computed.
- ✓ Each peer checks if the negative inclusions that he has collected are violated by the Data by sending queries to the corresponding peers.

P₁

$\text{Lang}_1 \subseteq \text{Course}_1$
 $\text{Math}_1 \subseteq \text{Course}_1$
 $\text{Lang}_1 \subseteq \neg \text{Math}_1$
 $\exists \text{TaughtTo}_1 \subseteq \text{Course}_1$
 $\exists \text{LangTaughtTo}_1 \subseteq \text{Lang}_1$
 $\exists \text{MathTaughtTo}_1 \subseteq \text{Math}_1$
 $\text{LangTaughtTo}_1 \subseteq \text{TaughtTo}_1$
 $\text{MathTaughtTo}_1 \subseteq \text{TaughtTo}_1$

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{Teach}_3^- \subseteq \text{Course}_1$

$\text{TaughtTo}_1(\text{Algebra, John})$

P₄

$\exists \text{PreparedBy}_4 \subseteq \text{Diploma}_4$
 $\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$
 $\text{PreparedBy}_4(\text{CS, Peter})$

P₂

$\text{ES}_2 \subseteq \text{Student}_2$
 $\exists \text{TaughtBy}_2 \subseteq \text{Student}_2$

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$
 $\text{Student}_2 \subseteq \neg \text{Teacher}_3$
 $\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

$\text{ES}_2(\text{Mike})$

P₃

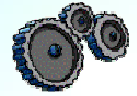
$\text{Mathematician}_3 \subseteq \text{Teacher}_3$
 $\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$

$\exists \text{Teach}_3^- \subseteq \text{Course}_1$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$
 $\text{Student}_2 \subseteq \neg \text{Teacher}_3$

$\text{Teach}_3(\text{John, Analysis})$

P₁

$Lang_1 \subseteq Course_1$
 $Math_1 \subseteq Course_1$
 $Lang_1 \subseteq \neg Math_1$
 $\exists TaughtTo_1 \subseteq Course_1$
 $\exists LangTaughtTo_1 \subseteq Lang_1$
 $\exists MathTaughtTo_1 \subseteq Math_1$
 $LangTaughtTo_1 \subseteq TaughtTo_1$
 $MathTaughtTo_1 \subseteq TaughtTo_1$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists Teach_3^- \subseteq Course_1$

$TaughtTo_1(Algebra, John)$

$\exists TaughtTo_1^- \subseteq Student_2$



P₂

$ES_2 \subseteq Student_2$
 $\exists TaughtBy_2 \subseteq Student_2$
 $\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$
 $\exists PreparedBy_4^- \subseteq Student_2$

ES_2 (Mike)

P₃

$Mathematician_3 \subseteq Teacher_3$
 $\exists Teach_3 \subseteq Mathematician_3$

$\exists Teach_3^- \subseteq Course_1$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$

$Teach_3$ (John, Analysis)

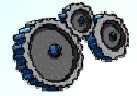
P₄

$\exists PreparedBy_4 \subseteq Diploma_4$
 $\exists PreparedBy_4^- \subseteq Student_2$

$PreparedBy_4(CS, Peter)$

P₁

$Lang_1 \subseteq Course_1$
 $Math_1 \subseteq Course_1$
 $Lang_1 \subseteq \neg Math_1$
 $\exists TaughtTo_1 \subseteq Course_1$
 $\exists LangTaughtTo_1 \subseteq Lang_1$
 $\exists MathTaughtTo_1 \subseteq Math_1$
 $LangTaughtTo_1 \subseteq TaughtTo_1$
 $MathTaughtTo_1 \subseteq TaughtTo_1$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists Teach_3^- \subseteq Course_1$

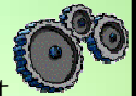
$TaughtTo_1(Algebra, John)$

P₄

$\exists PreparedBy_4 \subseteq Diploma_4$
 $\exists PreparedBy_4^- \subseteq Student_2$
 $PreparedBy_4(CS, Peter)$

P₂

$ES_2 \subseteq Student_2$
 $\exists TaughtBy_2 \subseteq Student_2$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$
 $\exists PreparedBy_4^- \subseteq Student_2$

$ES_2 (Mike)$

$Student_2 \subseteq \neg Teacher_3$

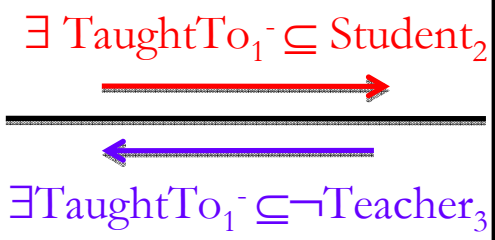


P₃

$Mathematician_3 \subseteq Teacher_3$
 $\exists Teach_3 \subseteq Mathematician_3$

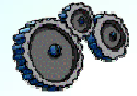
$\exists Teach_3^- \subseteq Course_1$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$

$Teach_3 (John, Analysis)$



P₁

$Lang_1 \subseteq Course_1$
 $Math_1 \subseteq Course_1$
 $Lang_1 \subseteq \neg Math_1$
 $\exists TaughtTo_1 \subseteq Course_1$
 $\exists LangTaughtTo_1 \subseteq Lang_1$
 $\exists MathTaughtTo_1 \subseteq Math_1$
 $LangTaughtTo_1 \subseteq TaughtTo_1$
 $MathTaughtTo_1 \subseteq TaughtTo_1$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists Teach_3^- \subseteq Course_1$

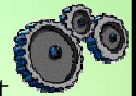
$TaughtTo_1(Algebra, John)$

P₄

$\exists PreparedBy_4 \subseteq Diploma_4$
 $\exists PreparedBy_4^- \subseteq Student_2$
 $PreparedBy_4(CS, Peter)$

P₂

$ES_2 \subseteq Student_2$
 $\exists TaughtBy_2 \subseteq Student_2$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$

$\exists TaughtTo_1^- \subseteq Student_2$



$\exists TaughtTo_1^- \subseteq \neg Teacher_3$ $paredBy_4^- \subseteq Student_2$

$\exists TaughtTo_1^- \subseteq \neg Mathematician_3$



$Student_2 \subseteq \neg Teacher_3$

$\exists TaughtTo_1^- \subseteq \neg Mathematician_3$



P₃

$Mathematician_3 \subseteq Teacher_3$
 $\exists Teach_3 \subseteq Mathematician_3$

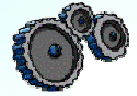
$\exists Teach_3^- \subseteq Course_1$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$



$Teach_3(John, Analysis)$

P₁

$Lang_1 \subseteq Course_1$
 $Math_1 \subseteq Course_1$
 $Lang_1 \subseteq \neg Math_1$
 $\exists TaughtTo_1 \subseteq Course_1$
 $\exists LangTaughtTo_1 \subseteq Lang_1$
 $\exists MathTaughtTo_1 \subseteq Math_1$
 $LangTaughtTo_1 \subseteq TaughtTo_1$
 $MathTaughtTo_1 \subseteq TaughtTo_1$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists Teach_3^- \subseteq Course_1$

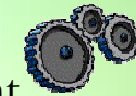
$TaughtTo_1(Algebra, John)$

P₄

$\exists PreparedBy_4 \subseteq Diploma_4$
 $\exists PreparedBy_4^- \subseteq Student_2$
 $PreparedBy_4(CS, Peter)$

P₂

$ES_2 \subseteq Student_2$
 $\exists TaughtBy_2 \subseteq Student_2$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$

$\exists TaughtTo_1^- \subseteq Student_2$

→

←

$\exists TaughtTo_1^- \subseteq \neg Teacher_3$ $PreparedBy_4^- \subseteq Student_2$

$\exists TaughtTo_1^- \subseteq \neg Mathematician_3$

$\exists TaughtTo_1^- \subseteq \neg \exists Teach_3$

$Student_2 \subseteq \neg Teacher_3$

$\exists TaughtTo_1^- \subseteq \neg Mathematician_3$

$\exists TaughtTo_1^- \subseteq \neg \exists Teach_3$



P₃

$Mathematician_3 \subseteq Teacher_3$
 $\exists Teach_3 \subseteq Mathematician_3$

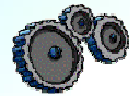
$\exists Teach_3^- \subseteq Course_1$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$



$Teach_3(John, Analysis)$

P₁

$Lang_1 \subseteq Course_1$
 $Math_1 \subseteq Course_1$
 $Lang_1 \subseteq \neg Math_1$
 $\exists TaughtTo_1 \subseteq Course_1$
 $\exists LangTaughtTo_1 \subseteq Lang_1$
 $\exists MathTaughtTo_1 \subseteq Math_1$
 $LangTaughtTo_1 \subseteq TaughtTo_1$
 $MathTaughtTo_1 \subseteq TaughtTo_1$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists Teach_3^- \subseteq Course_1$

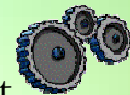
$TaughtTo_1(Algebra, John)$

P₄

$\exists PreparedBy_4 \subseteq Diploma_4$
 $\exists PreparedBy_4^- \subseteq Student_2$
 $PreparedBy_4(CS, Peter)$

P₂

$ES_2 \subseteq Student_2$
 $\exists TaughtBy_2 \subseteq Student_2$
 $\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$



$\exists TaughtTo_1^- \subseteq Student_2$



$\exists TaughtTo_1^- \subseteq \neg Teacher_3$ $paredBy_4^- \subseteq Student_2$

$\exists TaughtTo_1^- \subseteq \neg Mathematician_3$

$\exists TaughtTo_1^- \subseteq \neg \exists Teach_3$

$Student_2 \subseteq \neg Teacher_3$

$\exists TaughtTo_1^- \subseteq \neg Mathematician_3$

$\exists TaughtTo_1^- \subseteq \neg \exists Teach_3$



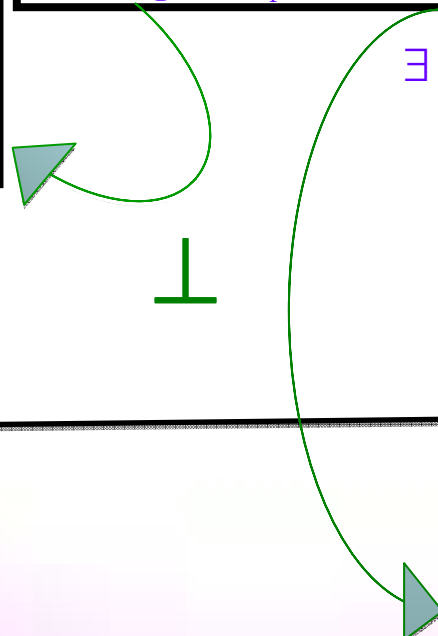
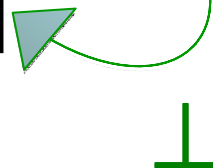
P₃

$Mathematician_3 \subseteq Teacher_3$
 $\exists Teach_3 \subseteq Mathematician_3$

$\exists Teach_3^- \subseteq Course_1$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$

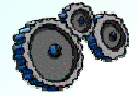


$Teach_3(John, Analysis)$



P₁

$Lang_1 \subseteq Course_1$
 $Math_1 \subseteq Course_1$
 $Lang_1 \subseteq \neg Math_1$
 $\exists TaughtTo_1 \subseteq Course_1$
 $\exists LangTaughtTo_1 \subseteq Lang_1$
 $\exists MathTaughtTo_1 \subseteq Math_1$
 $LangTaughtTo_1 \subseteq TaughtTo_1$
 $MathTaughtTo_1 \subseteq TaughtTo_1$



$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists Teach_3^- \subseteq Course_1$

$TaughtTo_1(Algebra, John)$

P₄

$\exists PreparedBy_4 \subseteq Diploma_4$
 $\exists PreparedBy_4^- \subseteq Student_2$
 $PreparedBy_4(CS, Peter)$

⊥

$\exists TaughtTo_1^- \subseteq Student_2$



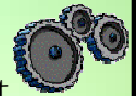
$\exists TaughtTo_1^- \subseteq \neg Teacher_3$

$\exists TaughtTo_1^- \subseteq \neg Mathematician_3$

$\exists TaughtTo_1^- \subseteq \neg \exists Teach_3$

P₂

$ES_2 \subseteq Student_2$
 $\exists TaughtBy_2 \subseteq Student_2$
 $\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$



$PreparedBy_4^- \subseteq Student_2$



$Student_2 \subseteq \neg Teacher_3$

$\exists TaughtTo_1^- \subseteq \neg Mathematician_3$

$\exists TaughtTo_1^- \subseteq \neg \exists Teach_3$



P₃

$Mathematician_3 \subseteq Teacher_3$
 $\exists Teach_3 \subseteq Mathematician_3$
 $\exists Teach_3^- \subseteq Course_1$
 $\exists TaughtBy_2^- \subseteq Teacher_3$
 $Student_2 \subseteq \neg Teacher_3$
 $Teach_3(John, Analysis)$



P₁

$\text{Lang}_1 \subseteq \text{Course}_1$
 $\text{Math}_1 \subseteq \text{Course}_1$
 $\text{Lang}_1 \subseteq \neg \text{Math}_1$
 $\exists \text{TaughtTo}_1 \subseteq \text{Course}_1$
 $\exists \text{LangTaughtTo}_1 \subseteq \text{Lang}_1$
 $\exists \text{MathTaughtTo}_1 \subseteq \text{Math}_1$
 $\text{LangTaughtTo}_1 \subseteq \text{TaughtTo}_1$
 $\text{MathTaughtTo}_1 \subseteq \text{TaughtTo}_1$

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{Teach}_3^- \subseteq \text{Course}_1$

$\text{TaughtTo}_1(\text{Algebra}, \text{John})$

⊥**OK****P₂**

$\text{ES}_2 \subseteq \text{Student}_2$
 $\exists \text{TaughtBy}_2 \subseteq \text{Student}_2$

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$
 $\text{Student}_2 \subseteq \neg \text{Teacher}_3$
 $\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

ES_2 (Mike)

P₄

$\exists \text{PreparedBy}_4 \subseteq \text{Diploma}_4$
 $\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

$\text{PreparedBy}_4(\text{CS}, \text{Peter})$

⊥**OK****P₃**

$\text{Mathematician}_3 \subseteq \text{Teacher}_3$
 $\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$

$\exists \text{Teach}_3^- \subseteq \text{Course}_1$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$
 $\text{Student}_2 \subseteq \neg \text{Teacher}_3$

Teach_3 (John, Analysis)

Query Answering

- Query Answering problem:

Given a **conjunctive query** q , compute the answers of q over the system.

- (Certain) Answer :

A tuple t of the constants appearing in KB such that:

$$\text{KB} \models q(t)$$

- In centralized case:

Algorithm **PerfectRef**: D.Calvenese and al. (JAR 07)

“Tractable reasoning and efficient query answering in description logics”

Data consistency checking

Query Answering

- Query Reformulation
- Reformulation Evaluation

Decentralized Query Answering

$P_1 \perp$

$\text{Lang}_1 \subseteq \text{Course}_1$	$\exists \text{TaughtTo}_1 \subseteq \text{Course}_1$
$\text{Math}_1 \subseteq \text{Course}_1$	$\exists \text{LangTaughtTo}_1 \subseteq \text{Lang}_1$
$\text{Lang}_1 \subseteq \neg \text{Math}_1$	$\exists \text{MathTaughtTo}_1 \subseteq \text{Math}_1$
$\text{LangTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{MathTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{TaughtTo}_1(\text{Algebra, John})$	

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$

OK

P_2

$\text{ES}_2 \subseteq \text{Student}_2$
$\exists \text{TaughtBy}_2 \subseteq \text{Student}_2$
$\text{ES}_2(\text{Mike})$
$\text{TaughtBy}_2(\text{Mike, Nada})$

$\exists \text{Teach}_3^- \subseteq \text{Course}_1$

$q(x) = \text{Student}_2(x)$

P_3

$\text{Mathematician}_3 \subseteq \text{Teacher}_3$
$\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$
$\text{Teach}_3(\text{John, Analysis})$

$\text{Student}_2 \subseteq \neg \text{Teacher}_3$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$

$\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

OK

P_4

$\exists \text{PreparedBy}_4 \subseteq \text{Diploma}_4$
$\text{PreparedBy}_4(\text{CS, Peter})$

Decentralized Query Answering

- Contribution:
 - Decentralized algorithm for query answering.
 - **Well Founded Answers** even in globally inconsistent Networks
 1. Decentralized Query Reformulation
 2. Checking data consistency w.r.t the peers involved in each reformulation
 - We keep only **sound** reformulations
 3. Evaluation of the sound reformulations
 - **Well founded answers**

Decentralized Query Answering

- Contribution:

- Decentralized algorithm for query answering.

- Query reformulation

- $q(x) = \text{Student}_2(x)$

Decentralized Query Answering

$P_1 \perp$

$\text{Lang}_1 \subseteq \text{Course}_1$	$\exists \text{TaughtTo}_1 \subseteq \text{Course}_1$
$\text{Math}_1 \subseteq \text{Course}_1$	$\exists \text{LangTaughtTo}_1 \subseteq \text{Lang}_1$
$\text{Lang}_1 \subseteq \neg \text{Math}_1$	$\exists \text{MathTaughtTo}_1 \subseteq \text{Math}_1$
$\text{LangTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{MathTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{TaughtTo}_1(\text{Algebra, John})$	

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$

OK

P_2

$\text{ES}_2 \subseteq \text{Student}_2$
$\exists \text{TaughtBy}_2 \subseteq \text{Student}_2$
$\text{ES}_2(\text{Mike})$
$\text{TaughtBy}_2(\text{Mike, Nada})$

$\exists \text{Teach}_3^- \subseteq \text{Course}_1$

$q(x) = \text{Student}_2(x)$

P_3

$\text{Mathematician}_3 \subseteq \text{Teacher}_3$
$\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$
$\text{Teach}_3(\text{John, Analysis})$

$\text{Student}_2 \subseteq \neg \text{Teacher}_3$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$

$\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

OK

P_4

$\exists \text{PreparedBy}_4 \subseteq \text{Diploma}_4$
$\text{PreparedBy}_4(\text{CS, Peter})$

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

Decentralized Query Answering

$P_1 \perp$

$Lang_1 \subseteq Course_1$	$\exists TaughtTo_1 \subseteq Course_1$
$Math_1 \subseteq Course_1$	$\exists LangTaughtTo_1 \subseteq Lang_1$
$Lang_1 \subseteq \neg Math_1$	$\exists MathTaughtTo_1 \subseteq Math_1$
$LangTaughtTo_1 \subseteq TaughtTo_1$	
$MathTaughtTo_1 \subseteq TaughtTo_1$	
$TaughtTo_1(Algebra, John)$	

$\exists TaughtTo_1^- \subseteq Student_2$
 $\exists LangTaughtTo_1^- \subseteq \neg ES_2$
 $\exists MathTaughtTo_1^- \subseteq Student_2$

OK

P_2

$ES_2 \subseteq Student_2$
$\exists TaughtBy_2 \subseteq Student_2$
$ES_2(Mike)$
$TaughtBy_2(Mike, Nada)$

$\exists Teach_3^- \subseteq Course_1$

$q(x) = Student_2(x)$

P_3

$Mathematician_3 \subseteq Teacher_3$
$\exists Teach_3 \subseteq Mathematician_3$
$Teach_3(John, Analysis)$

\perp

$Student_2 \subseteq \neg Teacher_3$
 $\exists TaughtBy_2^- \subseteq Teacher_3$

$\exists PreparedBy_4^- \subseteq Student_2$

OK

P_4

$\exists PreparedBy_4 \subseteq Diploma_4$
$PreparedBy_4(CS, Peter)$

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

$$q_2(x) = \exists z \text{ TaughtTo}_1(z, x)$$

Decentralized Query Answering

$P_1 \perp$

$\text{Lang}_1 \subseteq \text{Course}_1$	$\exists \text{TaughtTo}_1 \subseteq \text{Course}_1$
$\text{Math}_1 \subseteq \text{Course}_1$	$\exists \text{LangTaughtTo}_1 \subseteq \text{Lang}_1$
$\text{Lang}_1 \subseteq \neg \text{Math}_1$	$\exists \text{MathTaughtTo}_1 \subseteq \text{Math}_1$
$\text{LangTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{MathTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{TaughtTo}_1(\text{Algebra, John})$	

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$

OK

P_2

$\text{ES}_2 \subseteq \text{Student}_2$
$\exists \text{TaughtBy}_2 \subseteq \text{Student}_2$
$\text{ES}_2(\text{Mike})$
$\text{TaughtBy}_2(\text{Mike, Nada})$

$\exists \text{Teach}_3^- \subseteq \text{Course}_1$

$q(x) = \text{Student}_2(x)$

P_3

$\text{Mathematician}_3 \subseteq \text{Teacher}_3$
$\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$
$\text{Teach}_3(\text{John, Analysis})$

$\text{Student}_2 \subseteq \neg \text{Teacher}_3$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$

$\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

OK

P_4

$\exists \text{PreparedBy}_4 \subseteq \text{Diploma}_4$
$\text{PreparedBy}_4(\text{CS, Peter})$

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

$$q_2(x) = \exists z \text{ TaughtTo}_1(z, x)$$

$$q_3(x) = \exists y \text{ PreparedBy}_4(y, x)$$

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

$$q_2(x) = \exists z \text{ TaughtTo}_1(z, x)$$

$$q_3(x) = \exists y \text{ PreparedBy}_4(y, x)$$

- Data consistency checking

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

$$q_2(x) = \exists z \text{ TaughtTo}_1(z, x)$$

$$q_3(x) = \exists y \text{ PreparedBy}_4(y, x)$$

- Data consistency checking

Consistent algorithm on P_1 , P_2 and P_4

On P_1 : \perp

On P_2 : OK

On P_4 : OK

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

$$q_2(x) = \exists z \text{ TaughtTo}_1(z, x)$$

$$q_3(x) = \exists y \text{ PreparedBy}_4(y, x)$$

- Data consistency checking

Consistent algorithm on P_1 , P_2 and P_4

On P_1 : \perp

On P_2 : OK

On P_4 : OK

Query Evaluation

Decentralized Query Answering

$P_1 \perp$

$\text{Lang}_1 \subseteq \text{Course}_1$	$\exists \text{TaughtTo}_1 \subseteq \text{Course}_1$
$\text{Math}_1 \subseteq \text{Course}_1$	$\exists \text{LangTaughtTo}_1 \subseteq \text{Lang}_1$
$\text{Lang}_1 \subseteq \neg \text{Math}_1$	$\exists \text{MathTaughtTo}_1 \subseteq \text{Math}_1$
$\text{LangTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{MathTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{TaughtTo}_1(\text{Algebra, John})$	

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$

OK

P_2

$\text{ES}_2 \subseteq \text{Student}_2$
$\exists \text{TaughtBy}_2 \subseteq \text{Student}_2$
$\text{ES}_2(\text{Mike})$
$\text{TaughtBy}_2(\text{Mike, Nada})$

$\exists \text{Teach}_3^- \subseteq \text{Course}_1$

$q(x) = \text{Student}_2(x)$

P_3

$\text{Mathematician}_3 \subseteq \text{Teacher}_3$
$\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$
$\text{Teach}_3(\text{John, Analysis})$

$\text{Student}_2 \subseteq \neg \text{Teacher}_3$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$

$\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

OK

P_4

$\exists \text{PreparedBy}_4 \subseteq \text{Diploma}_4$
$\text{PreparedBy}_4(\text{CS, Peter})$

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

$$q_2(x) = \exists z \text{ TaughtTo}_1(z, x)$$

$$q_3(x) = \exists y \text{ PreparedBy}_4(y, x)$$



Query Evaluation

No answer

- Data consistency checking

Consistent algorithm on P_1 , P_2 and P_4

On P_1 : \perp

On P_2 : OK

On P_4 : OK

Decentralized Query Answering

$P_1 \perp$

$\text{Lang}_1 \subseteq \text{Course}_1$	$\exists \text{TaughtTo}_1 \subseteq \text{Course}_1$
$\text{Math}_1 \subseteq \text{Course}_1$	$\exists \text{LangTaughtTo}_1 \subseteq \text{Lang}_1$
$\text{Lang}_1 \subseteq \neg \text{Math}_1$	$\exists \text{MathTaughtTo}_1 \subseteq \text{Math}_1$
$\text{LangTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{MathTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{TaughtTo}_1(\text{Algebra}, \text{John})$	

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$

OK

P_2

$\text{ES}_2 \subseteq \text{Student}_2$
$\exists \text{TaughtBy}_2 \subseteq \text{Student}_2$
$\text{ES}_2(\text{Mike})$
$\text{TaughtBy}_2(\text{Mike}, \text{Nada})$

$\exists \text{Teach}_3^- \subseteq \text{Course}_1$

$q_1(x) = \text{ES}_2(x)$

P_3

$\text{Mathematician}_3 \subseteq \text{Teacher}_3$
$\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$
$\text{Teach}_3(\text{John}, \text{Analysis})$

\perp

$\text{Student}_2 \subseteq \neg \text{Teacher}_3$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$

$\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

OK

P_4

$\exists \text{PreparedBy}_4 \subseteq \text{Diploma}_4$
$\text{PreparedBy}_4(\text{CS}, \text{Peter})$

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

$$q_2(x) = \exists z \text{ TaughtTo}_1(z, x)$$

$$q_3(x) = \exists y \text{ PreparedBy}_4(y, x)$$

- Data consistency checking

Consistent algorithm on P_1 , P_2 and P_4

On P_1 : \perp

On P_2 : OK

On P_4 : OK

Query Evaluation

No answers

Well founded Answer = {Mike}

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

~~$$q_2(x) = \exists z \text{TaughtTo}_4(z, x)$$~~

$$q_3(x) = \exists y \text{PreparedBy}_4(y, x)$$

- Data consistency checking

Consistent algorithm on P_1 , P_2 and P_4

On P_1 : \perp

On P_2 : OK

On P_4 : OK

Query Evaluation

No answers

Well founded Answer= {Mike}

Decentralized Query Answering

$P_1 \perp$

$\text{Lang}_1 \subseteq \text{Course}_1$	$\exists \text{TaughtTo}_1 \subseteq \text{Course}_1$
$\text{Math}_1 \subseteq \text{Course}_1$	$\exists \text{LangTaughtTo}_1 \subseteq \text{Lang}_1$
$\text{Lang}_1 \subseteq \neg \text{Math}_1$	$\exists \text{MathTaughtTo}_1 \subseteq \text{Math}_1$
$\text{LangTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{MathTaughtTo}_1 \subseteq \text{TaughtTo}_1$	
$\text{TaughtTo}_1(\text{Algebra}, \text{John})$	

$\exists \text{TaughtTo}_1^- \subseteq \text{Student}_2$
 $\exists \text{LangTaughtTo}_1^- \subseteq \neg \text{ES}_2$
 $\exists \text{MathTaughtTo}_1^- \subseteq \text{Student}_2$

OK

P_2

$\text{ES}_2 \subseteq \text{Student}_2$
$\exists \text{TaughtBy}_2 \subseteq \text{Student}_2$
$\text{ES}_2(\text{Mike})$
$\text{TaughtBy}_2(\text{Mike}, \text{Nada})$

$\exists \text{Teach}_3^- \subseteq \text{Course}_1$

$q_3(x) = \exists y \text{PreparedBy}_4(y, x)$

P_3

$\text{Mathematician}_3 \subseteq \text{Teacher}_3$
$\exists \text{Teach}_3 \subseteq \text{Mathematician}_3$
$\text{Teach}_3(\text{John}, \text{Analysis})$

\perp

$\text{Student}_2 \subseteq \neg \text{Teacher}_3$
 $\exists \text{TaughtBy}_2^- \subseteq \text{Teacher}_3$

$\exists \text{PreparedBy}_4^- \subseteq \text{Student}_2$

OK

P_4

$\exists \text{PreparedBy}_4 \subseteq \text{Diploma}_4$
$\text{PreparedBy}_4(\text{CS}, \text{Peter})$

Decentralized Query Answering

- Contribution:

Decentralized algorithm for query answering.

- Query reformulation

$$q(x) = \text{Student}_2(x)$$

$$q_1(x) = \text{ES}_2(x)$$

$$\cancel{q_2(x) = \exists z \text{ TaughtTo}_4(z, x)}$$

$$q_3(x) = \exists y \text{ PreparedBy}_4(y, x)$$

- Data consistency checking

Consistent algorithm on P_1 , P_2 and P_4

On P_1 : \perp

On P_2 : OK

On P_4 : OK

Query Evaluation

No answers

Well founded Answer= {Mike}

Well founded Answer= {Peter}

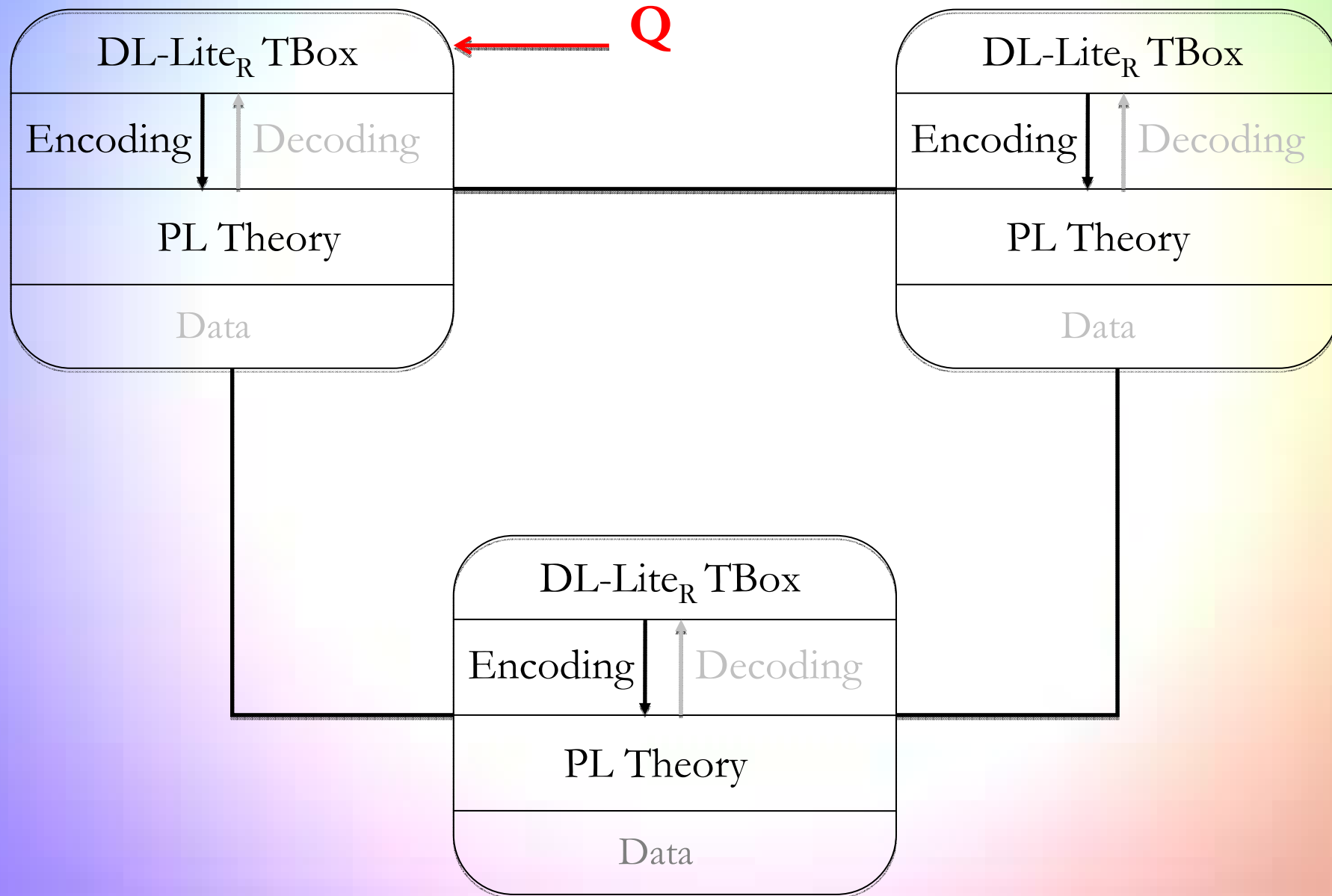
Decentralized query reformulation by using SomeWhere

- ✓ An existing Decentralized Infrastructure “SomeWhere” for reasoning in propositional logic and for which the experiments have demonstrated the scalability.

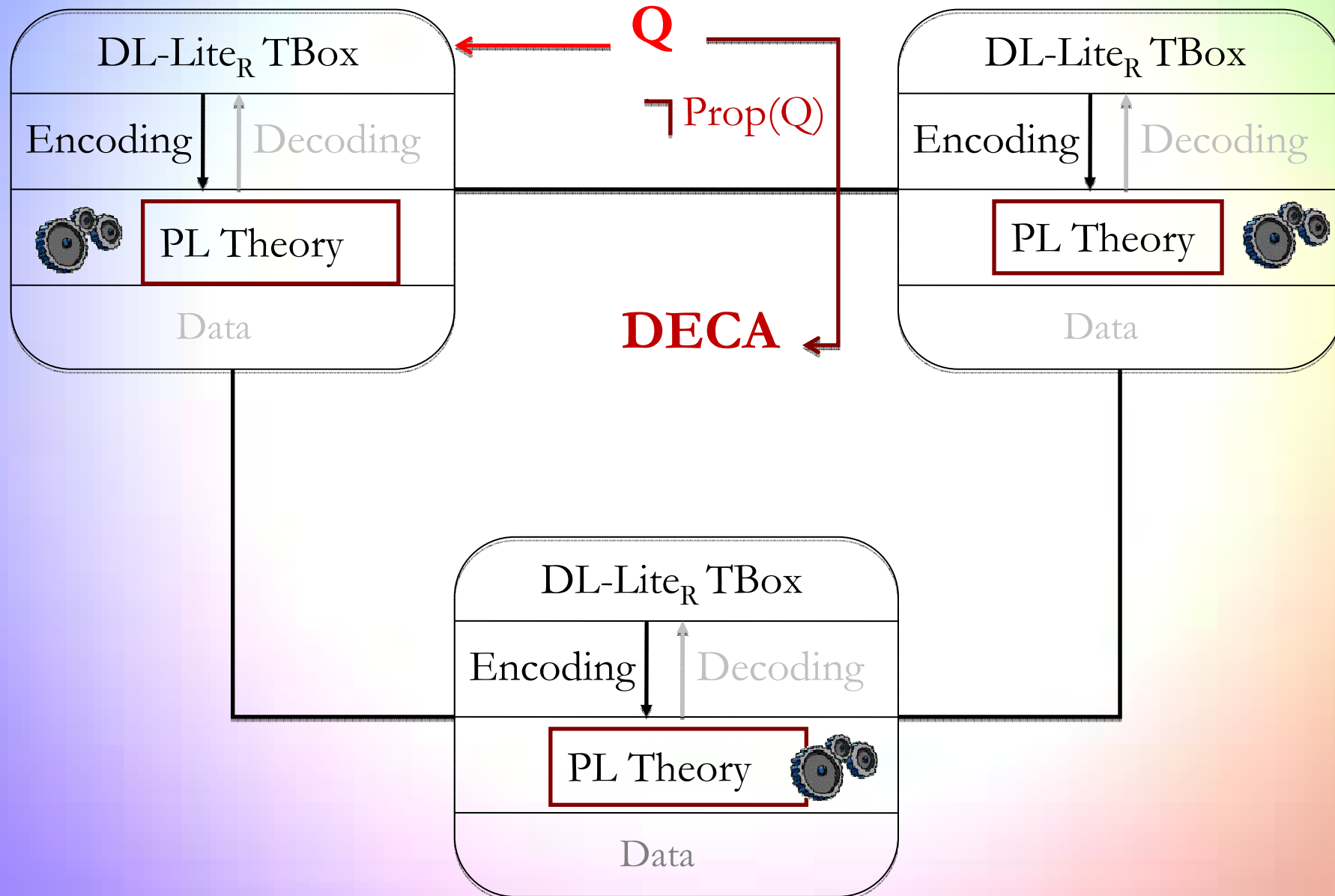
P. Adjiman and al. (IJCAI 05) : Scalability study of peer-to-peer consequence finding”

- ✓ An existing Decentralized Consequence finding Algorithm in propositional logic (DECA)
- ✓ A propositional encoding of the DL-Lite_R TBox.

Decentralized Query Reformulation by using SomeWhere

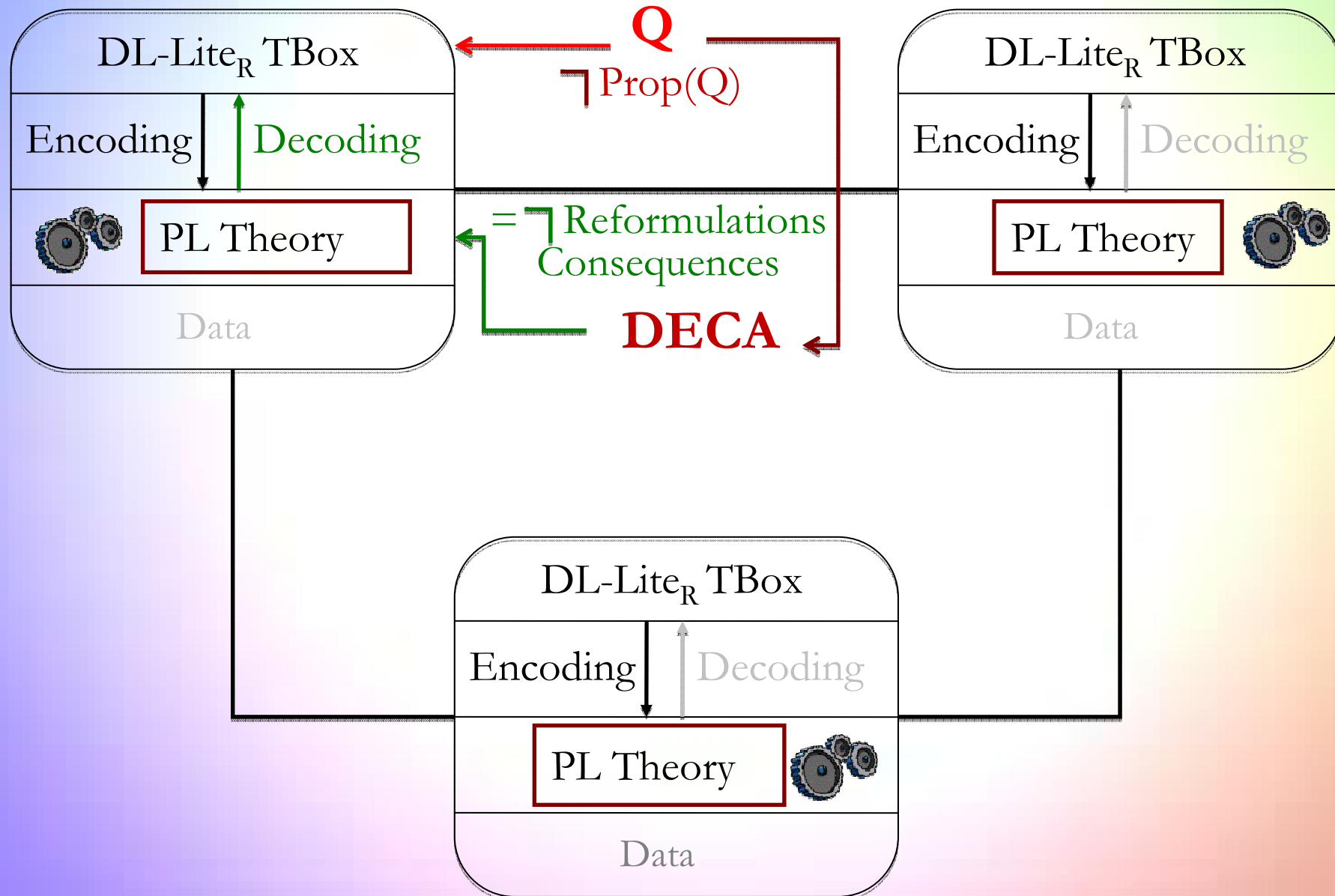


Decentralized Query Reformulation by using SomeWhere



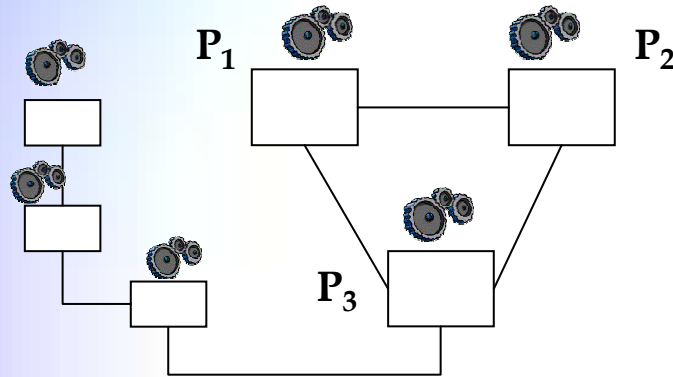
Decentralized Query Reformulation by using SomeWhere

Reformulations



Conclusion & future work

1. DL-Lite_R decentralized data model



2. Decentralized Algorithms for:

- ✓ Data consistency checking
- ✓ Query Answering

3. Decentralized & Centralized Algorithms for:

- ✓ View consistency checking
- ✓ Query Answering using views

Other Applications

- Mapping discovery:
Rémi Tournaire's PhD 2010
- Data reconciliation:
Extension of Fatiha Sais' PhD
- Explanation of answers
to queries

Feasibility of the approach with
other dialects of DL-Lite and
with Datalog+-